

CLAIMS

1. a countermeasure method for implementation in an electronic component implementing a public-key cryptography algorithm comprising exponentiation computation, with a left-to-right type exponentiation algorithm, of the type  $y=g^d$ , where  $g$  and  $y$  are elements of the determined group  $G$  written in multiplicative notation, and  $d$  is a predetermined number, said countermeasure method being characterized in that it includes a random draw step, at the start of or during execution of said exponentiation algorithm in deterministic or in probabilistic manner, so as to mask the accumulator  $A$ .

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2. A countermeasure method according to claim 1, characterized in that the group  $G$  is written in additive notation.

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3. A countermeasure method according to claim 1, characterized in that the group  $G$  is the multiplicative group of a finite field written  $GF(q^n)$ , where  $n$  is an integer.

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4. A countermeasure method according to claim 3, characterized in that the integer is  $n$  equal to 1:  $n=1$ .

5. A countermeasure method according to claim 4, characterized in that it comprises the following steps:

- 1) Determine an integer  $k$  defining the security of the masking and give  $d$  by the binary representation  $(d(t), d(t-1), \dots, d(0))$
  - 2) Initialize the accumulator  $A$  with the integer 1
  - 3) For  $i$  from  $t$  down to 0, do the following:
    - 3a) Draw a random integer  $\lambda$  lying in the range 0 to  $k-1$  and replace the accumulator  $A$  with  $A + \lambda \cdot q$  (modulo  $k \cdot q$ )
    - 3b) Replace  $A$  with  $A^2$  (modulo  $k \cdot q$ )
    - 3c) If  $d(i)=1$ , replace  $A$  with  $A \cdot g$  (modulo  $k \cdot q$ )
  - 4) Return  $A$  (modulo  $q$ ).
6. A countermeasure method according to claim 4, characterized in that it comprises the following steps:
- 1) Determine an integer  $k$  defining the security of the masking, and give  $d$  by the binary representation  $(d(t), d(t-1), \dots, d(0))$
  - 2) Draw a random integer  $\lambda$  lying in the range 0 to  $k-1$  and initialize the accumulator  $A$  with the integer  $1 + \lambda \cdot q$  (modulo  $k \cdot q$ )
  - 3) For  $i$  from  $t-1$  down to 0, do the following:
    - 3a) Replace  $A$  with  $A^2$  (modulo  $k \cdot q$ )
    - 3b) If  $d(i)=1$ , replace  $A$  with  $A \cdot g$  (modulo  $k \cdot q$ )
  - 4) Return  $A$  (modulo  $q$ ).

7. A countermeasure method according to claim 2, characterized in that the exponentiation algorithm applies to the group  $G$  of the points of an elliptic curve defined on the finite field  $GF(q^n)$ .

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8. A countermeasure method according to claim 7, characterized in that it comprises the following steps:

- 1) Initialize the accumulator  $A=(A_x, A_y, A_z)$  with the  $(x, y, 1)$  triplet and give  $d$  by the binary signed-digit representation  $(d(t+1), d(t), \dots, d(0))$  with  $d(t+1)=1$
- 2) For  $i$  from  $t$  down to  $0$ , do the following:
  - 2a) Draw a random non-zero element  $\lambda$  from  $GF(q^n)$  and replace the accumulator  $A=(A_x, A_y, A_z)$  with  $(\lambda^2.A_x, \lambda^3.A_y, \lambda.A_z)$
  - 2b) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$  in Jacobian representation, on the elliptic curve
  - 2c) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$  with  $(A_x, A_y, A_z)+d(i)*(x, y, 1)$  in Jacobian representation on the elliptic curve
- 3) If  $A_z=0$ , return the point at infinity; otherwise return  $(A_x/(A_z)^2, A_y/(A_z)^3)$ .

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9. A countermeasure method according to claim 7, characterized in that it comprises the following steps:

- 1) Draw a non-zero random element  $\lambda$  from  $GF(q^n)$  and initialize the accumulator  $A=(A_x, A_y, A_z)$  with the  $(\lambda^2.x, \lambda^3.y, \lambda)$  triplet and give  $d$  by

the binary signed-digit representation  
 $(d(t+1), d(t), \dots, d(0))$  with  $d(t+1)=1$

2) For  $i$  from  $t$  down to  $0$ , do the following:

2a) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$   
 5 in Jacobian representation, on the  
 elliptic curve

2b) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$   
 with  $(A_x, A_y, A_z)+d(i)*(x, y, 1)$  in Jacobian  
 representation on the elliptic curve

10 3) If  $A_z=0$ , return the point at infinity;  
 otherwise return  $(A_x/(A_z)^2, A_y/(A_z)^3)$ .

10. A countermeasure method according to claim 7,  
 characterized in that it comprises the following steps:

15 1) Initialize the accumulator  $A=(A_x, A_y, A_z)$  with  
 the  $(x, y, 1)$  triplet and give  $d$  by the binary  
 signed-digit representation  $(d(t+1), d(t), \dots,$   
 $d(0))$  with  $d(t+1)=1$

2) For  $i$  from  $t$  down to  $0$ , do the following:

20 2a) Draw a random non-zero element  $\lambda$  from  
 $GF(q^n)$  and replace the accumulator  
 $A=(A_x, A_y, A_z)$  with  $(\lambda.A_x, \lambda.A_y, \lambda.A_z)$

2b) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$   
 in homogeneous representation, on the  
 25 elliptic curve

2c) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$   
 with  $(A_x, A_y, A_z)+d(i)*(x, y, 1)$  in  
 homogeneous representation on the  
 elliptic curve

- 3) If  $A_z=0$ , return the point at infinity;  
otherwise return  $(A_x/A_z, A_y/A_z)$ .

11. A countermeasure method according to claim 7,  
5 characterized in that it comprises the following steps:

- 1) Draw a non-zero random element  $\lambda$  from  $GF(q^n)$   
and initialize the accumulator  $A=(A_x, A_y, A_z)$   
with the  $(\lambda.x, \lambda.y, \lambda)$  triplet and give  $d$  by the  
binary signed-digit representation  $(d(t+1),$   
10  $d(t), \dots, d(0))$  with  $d(t+1)=1$
- 2) For  $i$  from  $t$  down to  $0$ , do the following:
- 2a) Replace  $A=(A_x, A_y, A_z)$  with  $2*A=(A_x, A_y, A_z)$   
in homogeneous representation, on the  
elliptic curve
- 15 2b) If  $d(i)$  is non-zero, replace  $A=(A_x, A_y, A_z)$   
with  $(A_x, A_y, A_z) + d(i) * (x, y, 1)$  in  
homogeneous representation on the  
elliptic curve
- 3) If  $A_z=0$ , return the point at infinity;  
20 otherwise return  $(A_x/A_z, A_y/A_z)$ .

12. An electronic component using the  
countermeasure method according to any preceding claim.